DSE3-N Metric Spaces And Complex Analysis

1. Basic Notions

- 1.1 Definition and examples
- 1.2 Open Balls and Open Sets

2. Convergence

- 2.1 Convergent Sequences
- 2.2 Limit and Cluster points
- 2.3 Cauchy Sequences and Completeness
- 2.4 Bounded Sets
- 2.5 Dense Sets
- 2.6 Boundary of a set

3. Continuity

- 3.1 Continuous Functions
- 3.2 Equivalent Definitions of Continuity
- 3.3 Topological Property
- 3.4 Uniform Continuity
- 3.5 Limit of a Function
- 3.6 Open and closed maps

4. Compactness and Connectedness

- 4.1 Compact Spaces and their Properties
- 4.2 Connected Spaces

5: Analytic functions

5.1.Functions of a Complex Variables

5.2.Limits, Theorems on limits (Without Proof), Limits involving the point at infinity,

Continuity, Derivatives, Differentiation formulas (Without Proof)

5.3.Cauchy- Riemann Equations, Sufficient Conditions for differentiability (Only Statement and Examples)

5.4.Polar coordinates, Analytic functions, Harmonic functions.

6: Elementary Functions

6.1 The Exponential functions

6.2 The Logarithmic function, Branches and derivatives of logarithms, Some identities involving logarithms

6.3 Complex exponents, Trigonometric functions.

7. Integrals

7.1 Derivatives of functions, Definite integrals of functions

7.2 Contours, Contour integral, Examples

7.3 Upper bounds for Moduli of contour integrals, Anti-derivatives (Only Examples)

7.4 Cauchy-Goursat Theorem (without proof), Simply and multiply Connected domains. Cauchy integral formula, Derivatives of analytic functions. Liouville's Theorem and Fundamental Theorem of Algebra (Without Proof).

8. Series

8.1 Convergence of sequences and series (Theorems without proof)

8.2 Taylor's series (without proof), Laurent series (without proof), examples only.

9. Residues and Poles

9.1 Isolated singular points, Residues

9.2 Cauchy residue theorem (Without Proof), residue at infinity, types of isolated singular points, residues at poles

9.3 Zeros of analytic functions, zeros and poles.